

Recent results of new mbtrack

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Supplement

Optimum condition of double RF system

$$V(\phi) = V_{fc} \left\{ \cos(\phi + \phi_{fc}) + k \cos(m\phi + \phi_{hc}) \right\}$$

$$V(0) = U_{Loss} / e$$

$$V'|_0 = \alpha, V''|_0 = 0$$

$$\cos \phi_{fc} = \frac{m^2}{m^2 - 1} \frac{U_{Loss}}{eV_{fc}}$$

$$\tan \phi_{hc} = m \frac{\alpha / eV_{fc} + \sin \phi_{fc}}{\cos \phi_{fc}}$$

$$k = - \frac{\cos \phi_{fc}}{m^2 \cos \phi_{hc}}$$

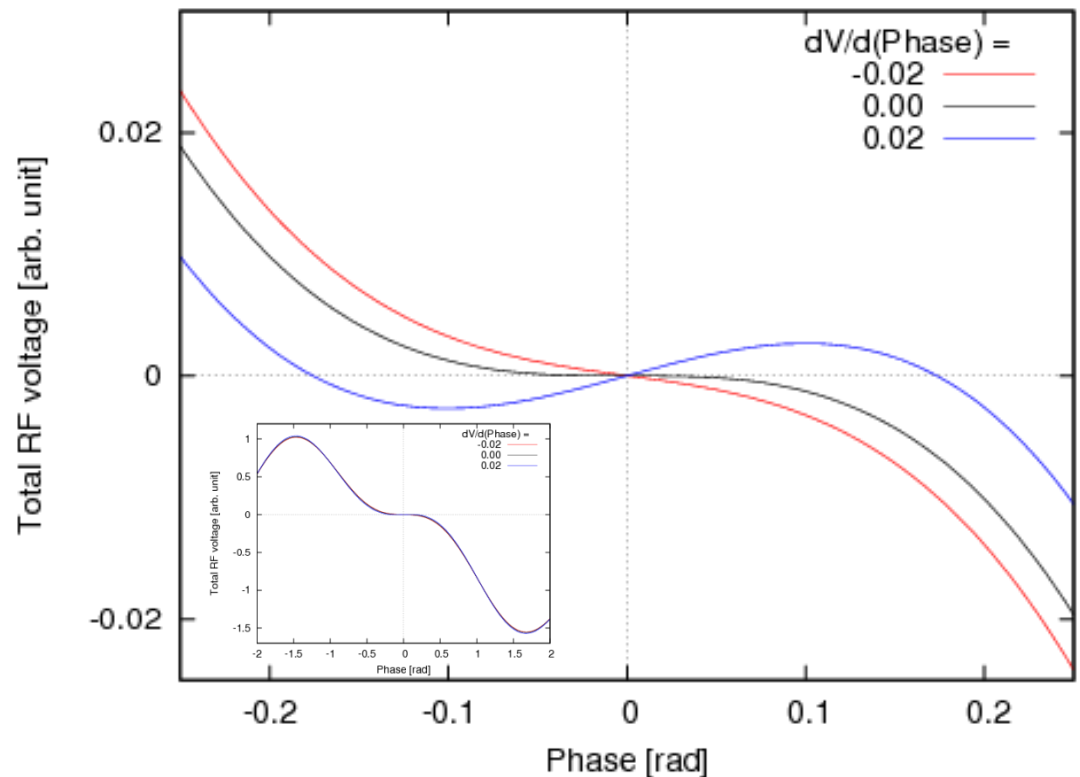
V_{fc} : main voltage, m : harmonics

U_{loss} : radiation loss per turn

k : ratio of main and harmonic voltage

ϕ_{fc} : main RF phase

ϕ_{hc} : harmonic RF phase



Active harmonic cavity (ESRF)

Principal parameters of ESRF-EBS

RF frequency	f_{rf}	(MHz)	352,370
Harmonics number	h		992
Revolutoin frequency	f_{rev}	(MHz)	0,355
Main rf voltage	V_c	(MV)	6,6
Radiation loss per turn	U_o	(MeV/turn)	3,200

Parameters of Harmonic cavity

Shunt Impedance [$M\Omega$]	R_a	5,8
Quality factor	Q_o	20000
R/Q [Ω], $R=V_c^2/P_c$	R/Q	290

*R/Q seems higher.

Tracking parameters for Harmonic cavities at stored currents of 200mA

Harmonic cavity voltage	k	0,286	0,286	0,286	0,286
Main cavity phase (cosine)	ϕ_s	56,9	56,9	56,9	56,9
Harmonic cavity phase (cosine)	ϕ_n	-102,24	-102,24	-102,24	-102,24
Number of harmonic cavities	N_{hc}	5	5	5	5
Cavity coupling factor	β_{hc}	0,3483	1,000000	2,000000	5,000000
Total dissipation [kW]	$P_{c,hc}$	122,759	122,759	122,759	122,759
Beam loading power [kW]	$P_{b,hc}$	-80,0	-80,0	-80,0	-80,0
Total reflection power [kW]	$P_{r,hc}$	0,00	13,03	41,86	132,81
Total generator power [kW]	$P_{g,hc}$	42,8	55,8	84,6	175,6
Detuning frequency [kHz]	δf_{hc}	75,103	75,103	75,1	112,7
K-value, $f_s \approx V(K)$	K	1,49	0,68	-0,42	-2,16

Optimum coupling

Active harmonic cavity (ESRF)

Filling : Uniform,7/8 fill Damping time: * ms
Stored current : 200mA
With Harmonic cavity

$$V(\phi) = V_{fc} \left\{ \cos(\phi + \phi_{fc}) + k \cos(m\phi + \phi_{hc}) \right\}$$
$$V(0) = U_{Loss} / e$$
$$V'|_0 = \alpha, V''|_0 = 0$$

Summary of the calculation results

Comment	Stable or not at each damping time								K*	CBI Growth time** [ms]			
	0,1	0,5	1,0	1,5	2,0	3,0	4.0	8,6ms		l=0 real	l=1 real	l=1 imag	
Optimum (flat potential), uniform fill	Unstable (Bunch length)								1,50	-8,58	24,75	0,82	
slope -0.01, uniform fill	Stable								1,80		24,57	0,82	
slope -0.02, uniform fill									2,07		25,04	0,81	
Coupling Beta = 5, 7/8 fill									-2,16	-6,60	4,97	0,95	
Coupling Beta = 2, 7/8 fill									-0,42	-7,82	11,98	0,85	
Coupling Beta = 1, 7/8 fill	Unstable or Beam lost								0,69	-8,57	16,96	0,83	
Optimum tuning, (not flat) 7/8 fill									1,50	-8,58	24,75	0,82	
Coupling Beta = 0.1, 7/8 fill	Stable								1,67	-8,46	27,79	0,82	
Coupling Beta = 0.2, 7/8 fill									1,78	-8,34	30,34	0,82	

*f_s = sqrt(K) **Assuming with Ω_s≈ω_s

Active harmonic cavity (ESRF)

Filling : Uniform, 7/8 fill Damping time: * ms
 Stored current : 200mA
 With Harmonic cavity

$$V(\phi) = V_{fc} \left\{ \cos(\phi + \phi_{fc}) + k \cos(m\phi + \phi_{hc}) \right\}$$

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Coupling Beta = 0.2, 7/8 fill									1,78	-8,34	30,34	0,82
	Stable											

Two different source of the instabilities?

- 1.(violet) RF flat potential (disappearance of focusing force)
- 2.(red) Harmonic Cavity(high-Q) impedances

Active harmonic cavity (ESRF)

Stored current : 200mA

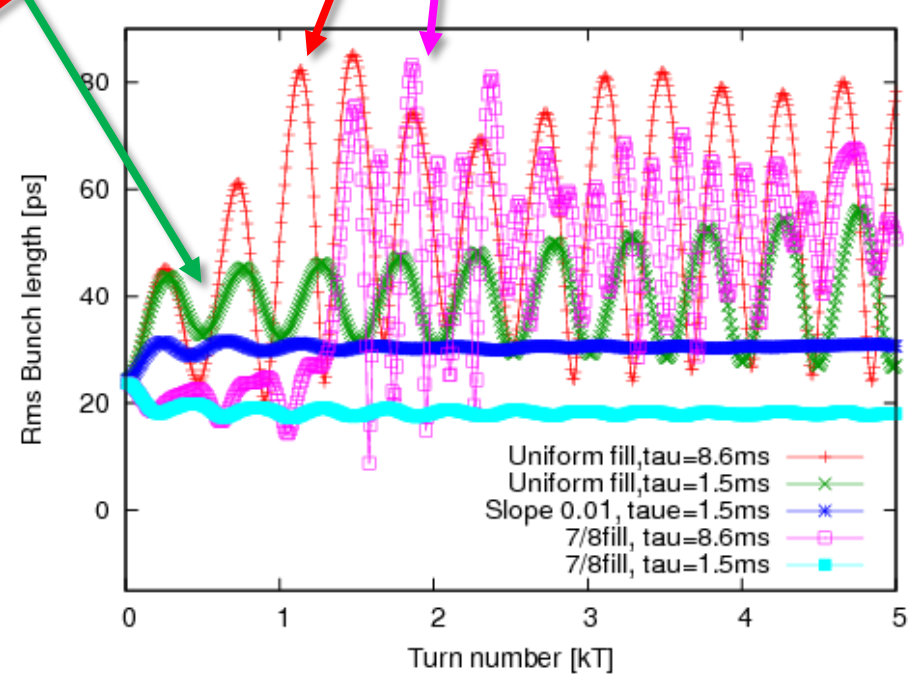
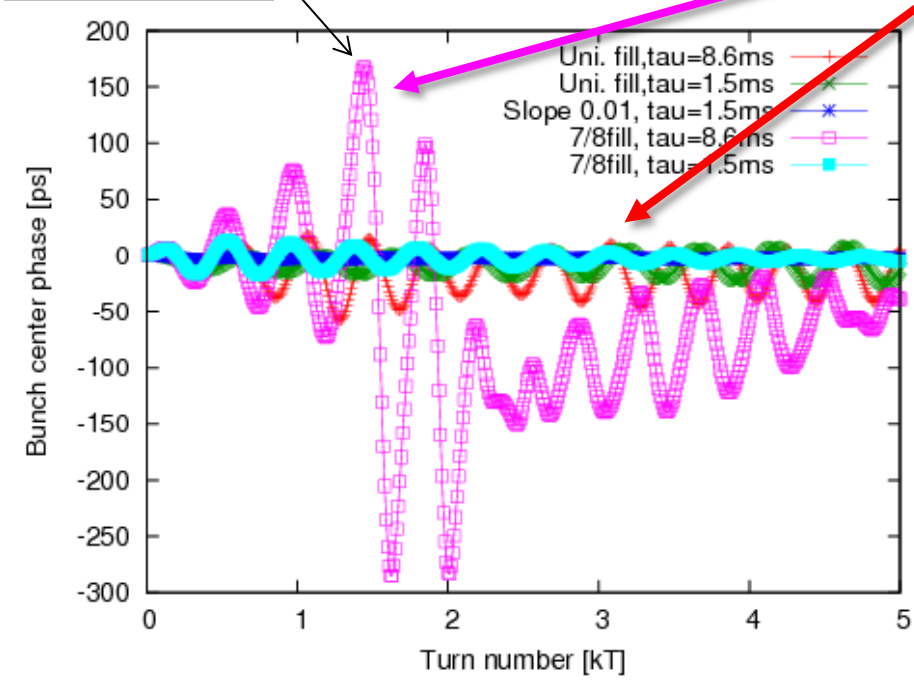
Summary of the calculation results

Comment	Stable or not at each damping time									
	0,1	0,5	1,0	1,5	2,0	3,0	4,0			8,6ms
Optimum (flat potential), uniform fill slope -0.01, slope -0.02,										
Optimum tuning, (not flat) Coupling Beta = 0.1, Coupling Beta = 0.2,										

Unstable bunch shape
(bunch length)

Beam unstable
(coherent motion)

Beam lost here

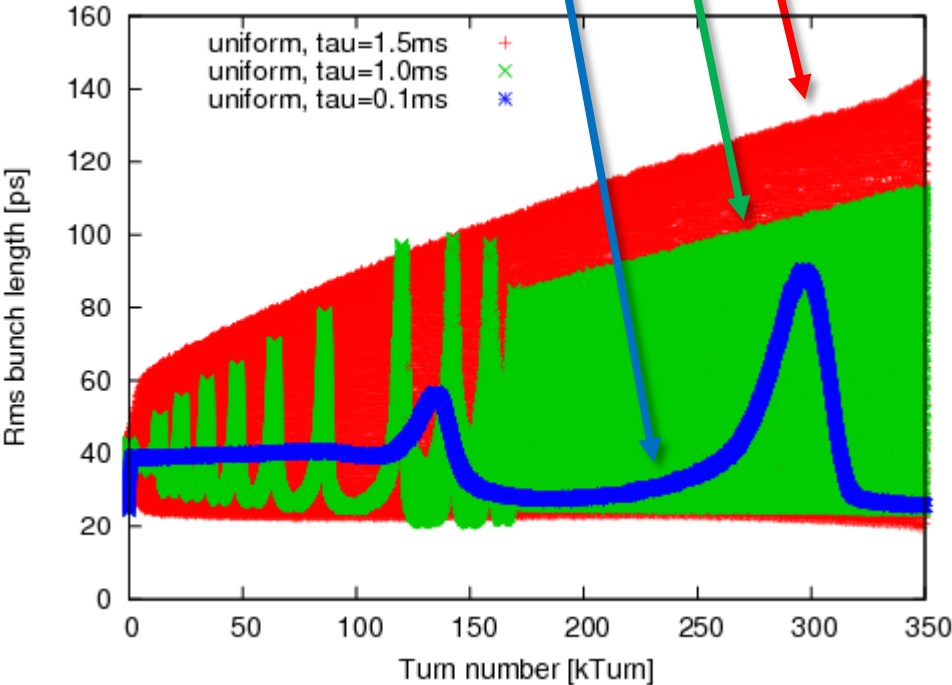


Active harmonic cavity (ESRF)

Stored current : 200mA

Summary of the calculation results

Comment	Stable or not at each damping time							
	0,1	0,5	1,0	1,5	2,0	3,0	4,0	8,6ms
Optimum (flat potential), uniform fill slope -0.01, slope -0.02,	uniform fill	uniform fill	uniform fill	uniform fill	uniform fill	uniform fill	uniform fill	uniform fill
Optimum tuning, (not flat)	7/8 fill	7/8 fill	7/8 fill	7/8 fill	7/8 fill	7/8 fill	7/8 fill	7/8 fill
Coupling Beta = 0.1,	7/8 fill	7/8 fill	7/8 fill	7/8 fill	7/8 fill	7/8 fill	7/8 fill	7/8 fill
Coupling Beta = 0.2,	7/8 fill	7/8 fill	7/8 fill	7/8 fill	7/8 fill	7/8 fill	7/8 fill	7/8 fill



Typical tracking results
for the flat-potential induced instabilities
(unstable bunch shape)



Before the continuous unstable motion
(in case of Growth rate \approx Damping rate),
Bunch length values are oscillated.

It looks like quadrupole mode.

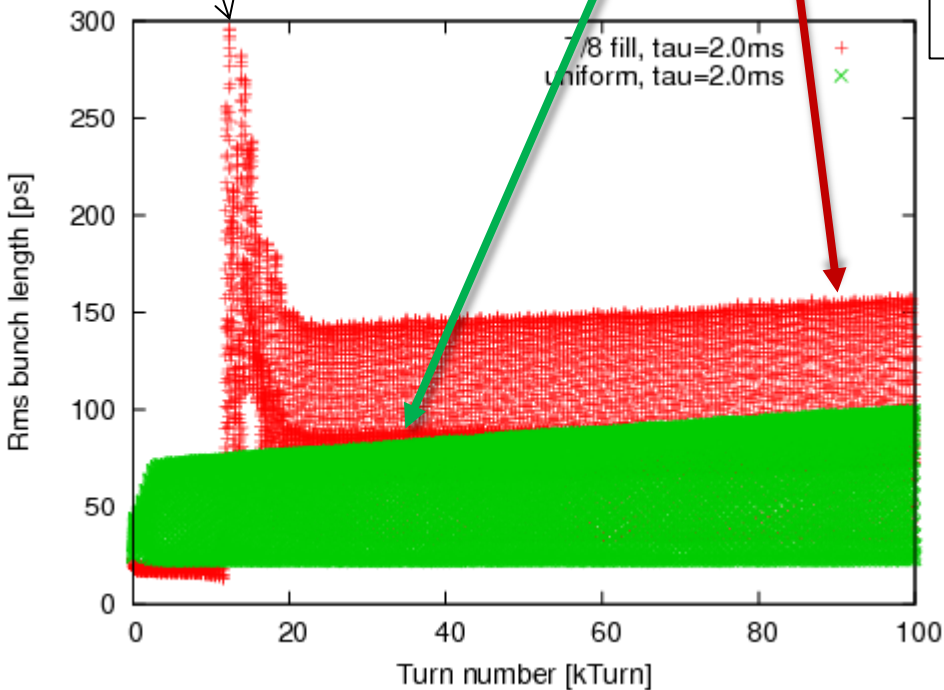
Active harmonic cavity (ESRF)

Stored current : 200mA

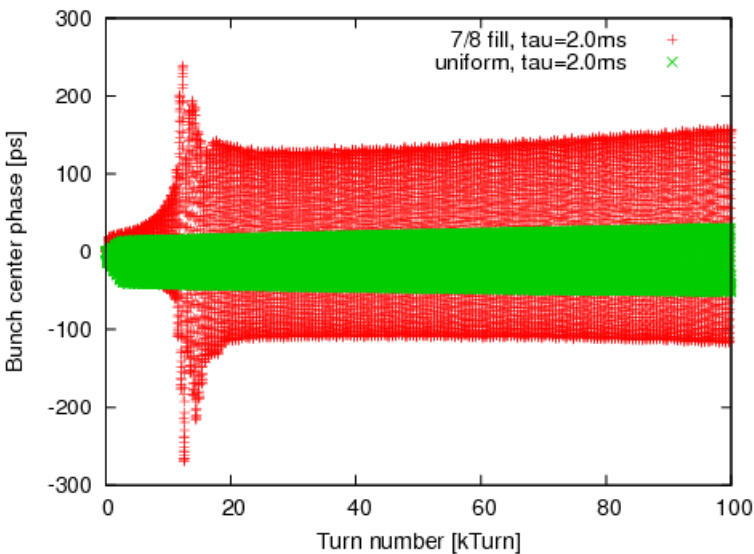
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Optimum (flat potential), uniform fill slope -0.01, slope -0.02,										
Optimum tuning, (not flat) Coupling Beta = 0.1, Coupling Beta = 0.2,	7/8 fill									
	7/8 fill									
	7/8 fill									

Beam lost here



Comparison of two different instabilities



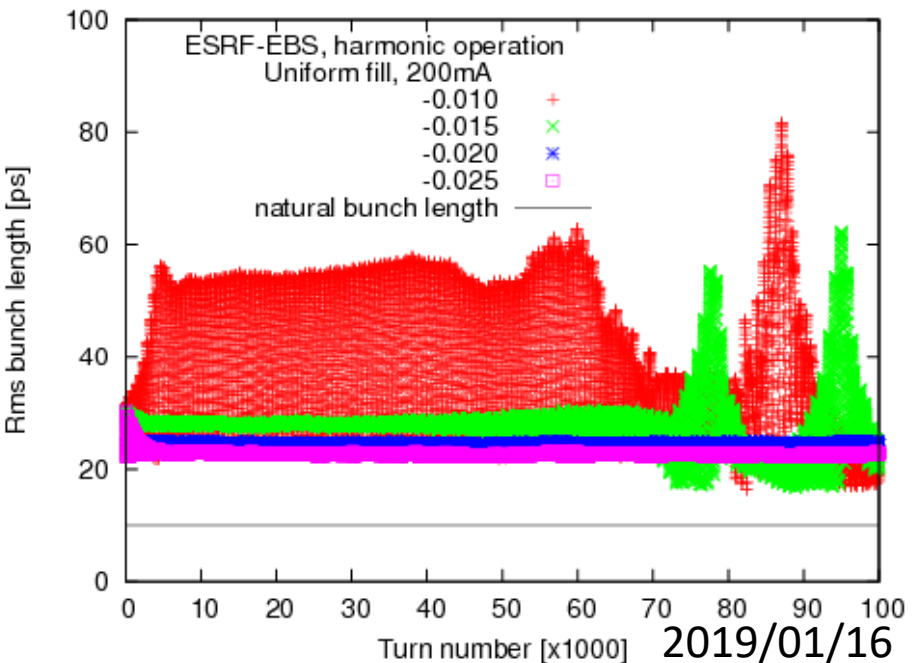
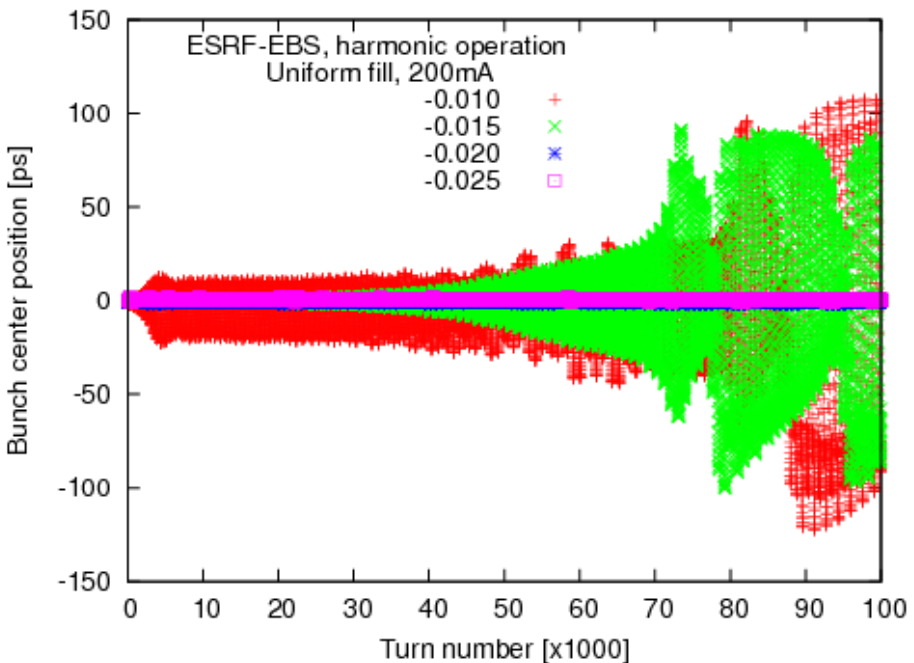
1.Instability in flat potential condition (ESRF, uniform)

Comment	Stable or not at each damping time							
	0,1	0,5	1,0	1,5	2,0	3,0	4.0	8,6ms
Optimum (flat pot.), uni. Fill								
slope -0.01, uni. Fill								
slope -0.02, uni. fill								

$$V(\phi) = V_{fc} \left\{ \cos(\phi + \phi_{fc}) + k \cos(m\phi + \phi_{hc}) \right\}$$
$$V(0) = U_{Loss} / e$$
$$V'|_0 = \alpha, V''|_0 = 0$$

- In the flat potential conditions, the beam shape is fluctuated(Red).
- Adding residual slopes to the rf potential, the beam becomes stable (Blue and Magenta).

Filling : Uniform Damping time: 8.6 ms
Stored current : 200mA



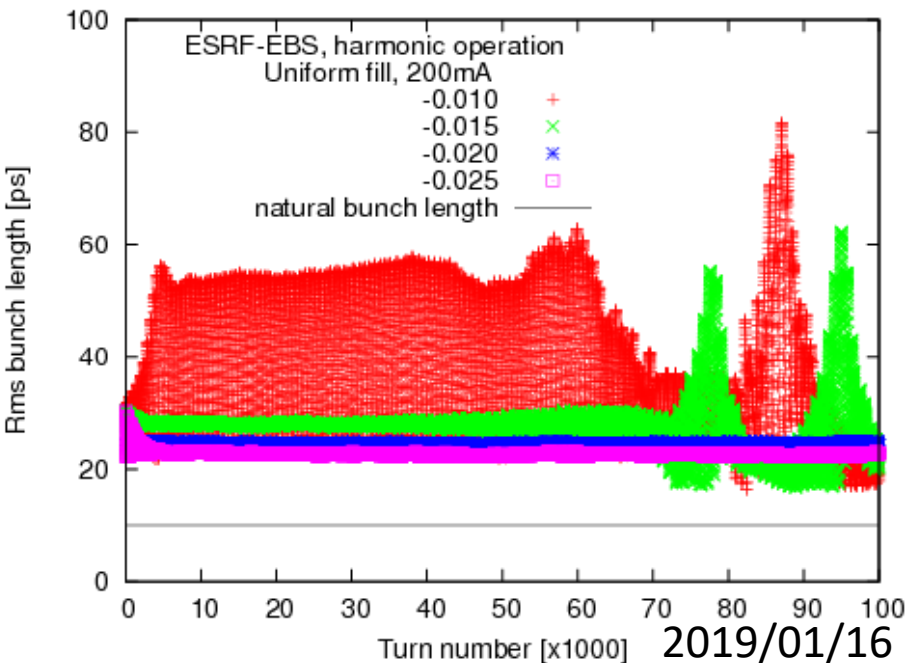
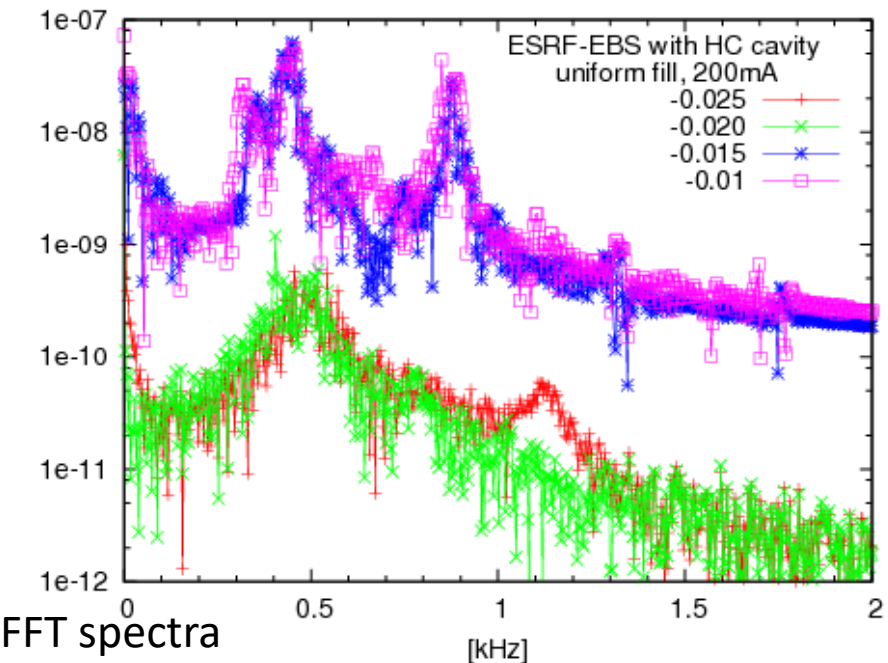
1.Instability in flat potential condition (ESRF, uniform)

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	0,1	0,5	1,0	1,5	2,0	3,0	4.0	8,6ms
Optimum (flat pot.), uni. Fill								
slope -0.01, uni. Fill								
slope -0.02, uni. fill								

$$V(\phi) = V_{fc} \left\{ \cos(\phi + \phi_{fc}) + k \cos(m\phi + \phi_{hc}) \right\}$$
$$V(0) = U_{Loss} / e$$
$$V'|_0 = \alpha, V''|_0 = 0$$

- In the flat potential conditions, the beam shape is fluctuated(Red).
- Adding residual slopes to the rf potential, the beam becomes stable (Blue and Magenta).

Filling : Uniform Damping time: 8.6 ms
Stored current : 200mA



2. Instability due to cavity impedances cavity(?) (ESRF)

Summary of the calculation results

Comment	Stable or not at each damping time								K*	CBI Growth time** [ms]		
	0,1	0,5	1,0	1,5	2,0	3,0	4.0	8,6ms		l=0 real	l=1 real	l=1 imag
Optimum (flat potential), uniform fill	Unstable (Bunch length)								1,50	-8,58	24,75	0,82
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Optimum tuning, (not flat) 7/8 fill									1,50	-8,58	24,75	0,82
Coupling Beta = 0.1, 7/8 fill	Stable								1,67	-8,46	27,79	0,82
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What is the source of these instabilities?

a) Robinson instability?

$$f_s \sim f_{rf} \times \text{sqrt} [\alpha K'], \quad (K' < 0 \Leftrightarrow \text{DC Robinson instability})$$
$$K' = V_c \sin \phi_s + V_b \sin \psi + 3 V_{c,3} \sin \phi_{s,3} + 3 V_{b,3} \sin \psi \quad (\text{cosine-definition for } \phi_s \text{ \& } \phi_{s,3})$$

b) l=1 mode instabilities (Venturini's paper)

Passive harmonic cavity (SLS, uniform)

SLS parameter, $I_0 = 320$ mA

Damping time = 4,5 ms

[cavity_resonator_1]

$m = 1.0$

$R_s = 13.6e6$

$Q_{zero} = 40000.0$

$Q_{load} = 9302$

$V_c = 2.0e6$

$syncPhase = 1.2680686$

$FBmode = 1$

$FBGain = 1$

$ForceWR = 1$

[cavity_resonator_2]

$m = 3.0$

$R_s = 1.7648e10$

$Q_{zero} = 2.0e8$, $Q_{load} = 109208.77$

#optimum# $V_c = 0.63979e6$, $syncPhase = -1.67453179$

slope -1% # $V_c = 0.62653041e6$, $syncPhase = -1.6767355$

slope -2% # $V_c = 0.61327345e6$, $syncPhase = -1.6790344$

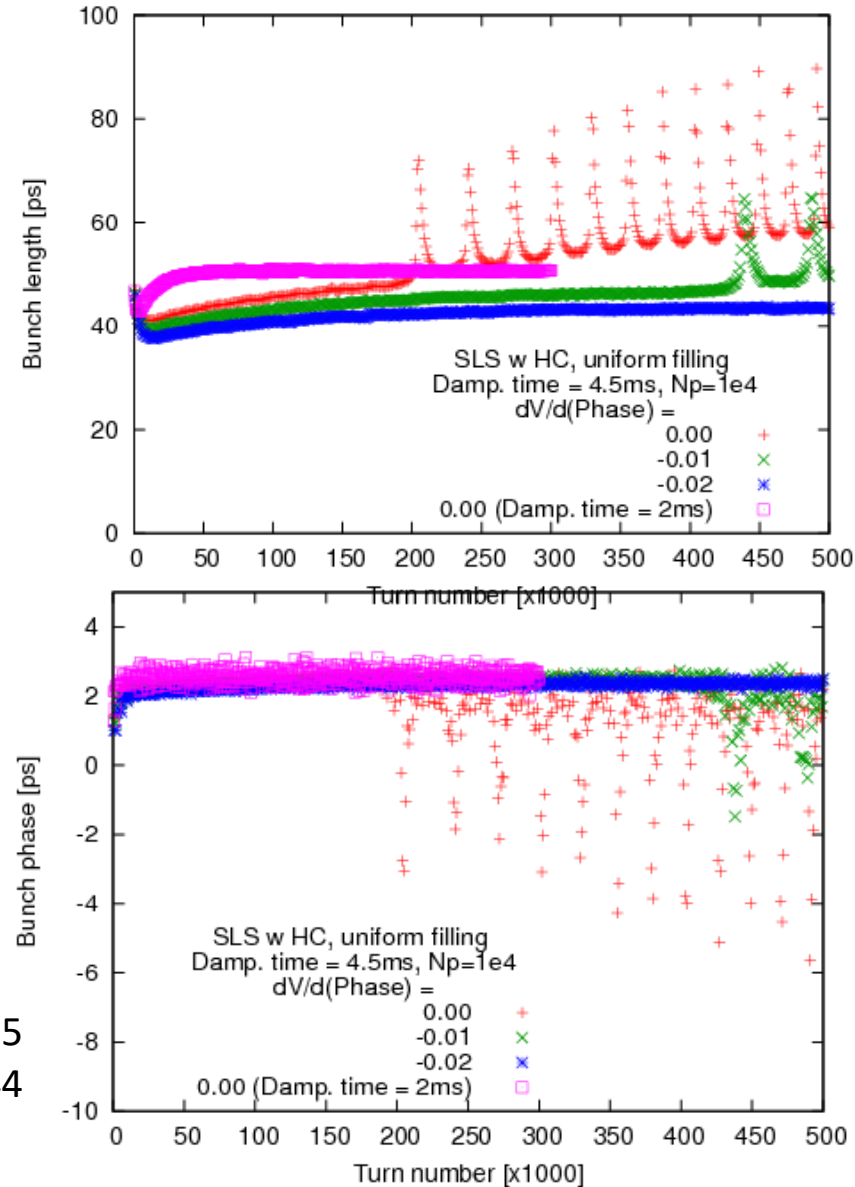
$geneVolt = 0.0$

$FBmode = 2$, $FBgain = 0.1$

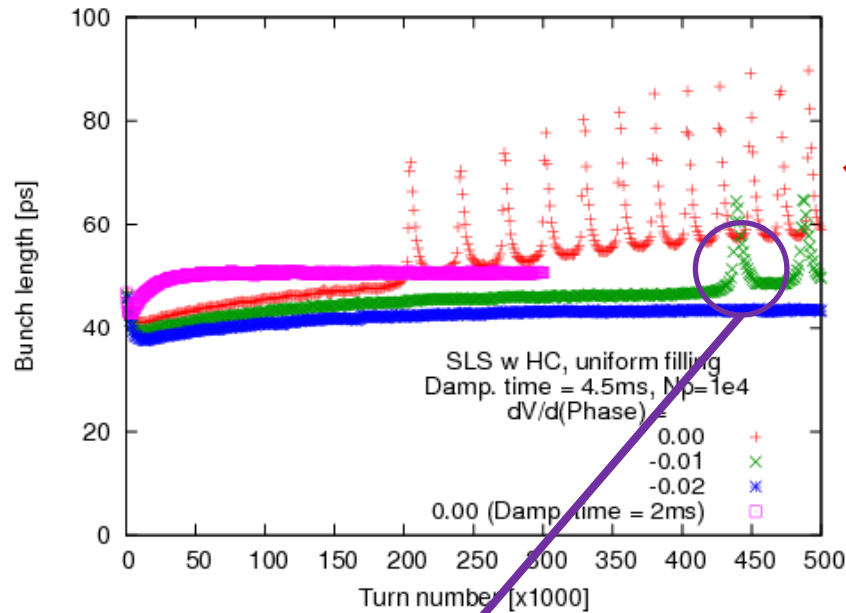
$ForceWR = 1$

Bunch length (Anal.) :
50,9 ps (x3,74)

Flat potential
-> unstable beam?



Passive harmonic cavity (SLS, uniform)

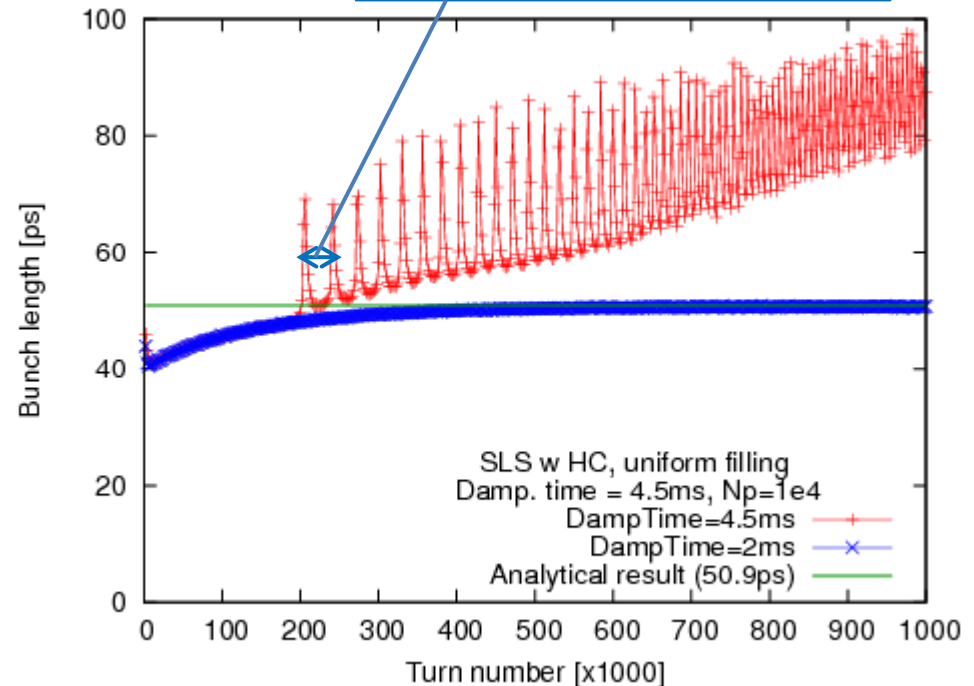


Bunch length (Anal.) : 50,9 ps (x3,74)

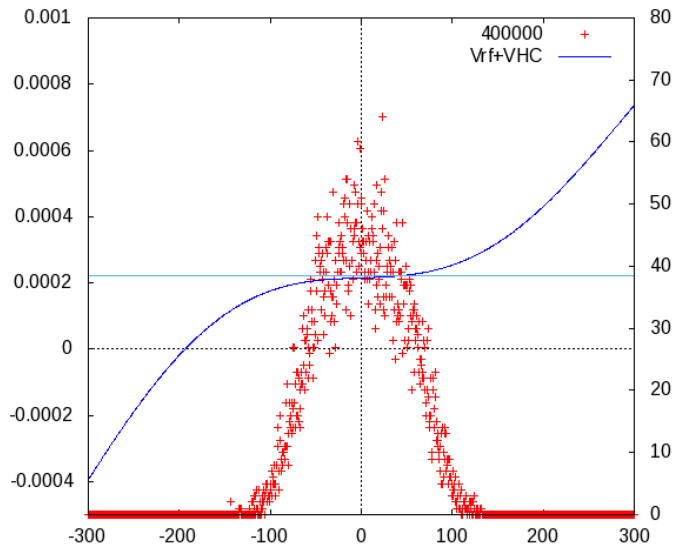
$f_{s0} = 6.6\text{kHz}$
 $\tau_{cav} = 5.9\mu\text{s}$

More turn

36 turn (34.6us, 28.9kHz)



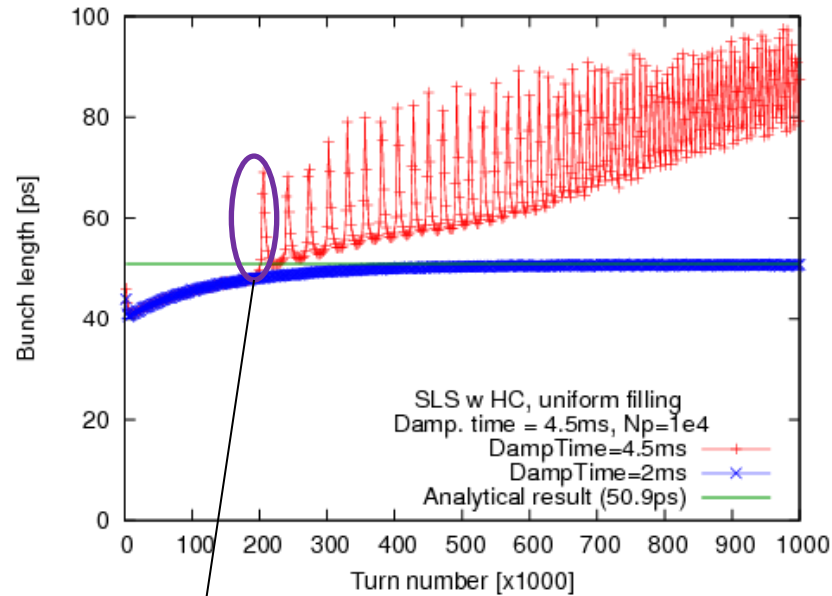
Bunch profiles



Quadratic mode?

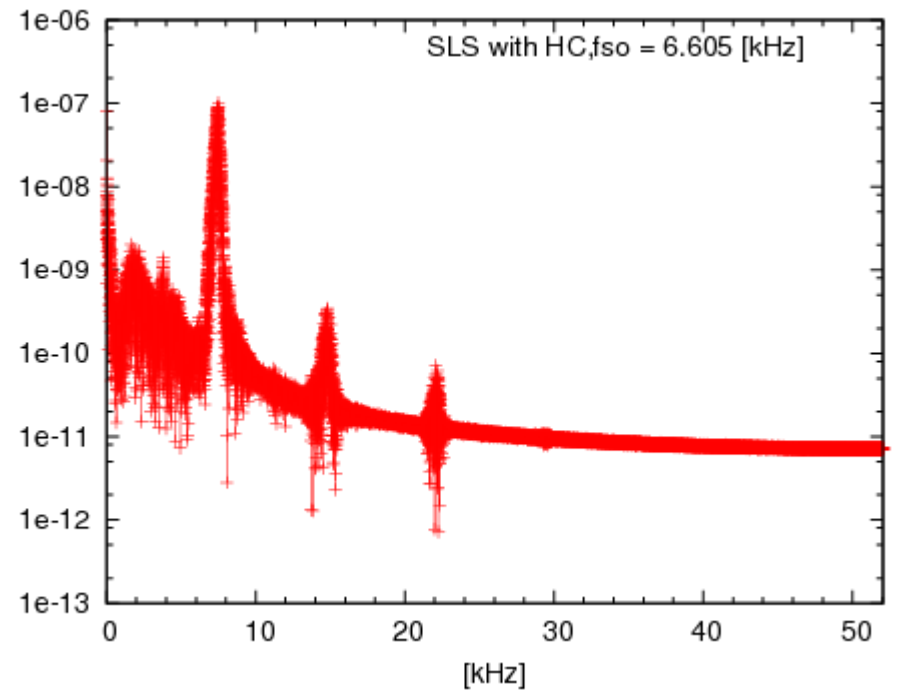
2018/11/28

Passive harmonic cavity (SLS, uniform)



Growth rate = 38 [1/s] (26ms)
* with damp. time (4.5ms)

FFT



$f_{s0} = 6.6 \text{ kHz}$
 $\tau_{cav} = 5.9 \mu\text{s}$